## What is claimed is:

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- 1. A method for making a glass-ceramic, the method comprising heat-treating glass to convert at least a portion of the glass to crystalline ceramic and provide glass-ceramic, the glass comprising at least 35 percent by weight Al<sub>2</sub>O<sub>3</sub>, based on the total weight of the glass, REO, at least one of ZrO<sub>2</sub> or HfO<sub>2</sub>, and at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub>, wherein the glass contains not more than 10 percent by weight collectively As<sub>2</sub>O<sub>3</sub>, B<sub>2</sub>O<sub>3</sub>, GeO<sub>2</sub>, P<sub>2</sub>O<sub>5</sub>, SiO<sub>2</sub>, TeO<sub>2</sub>, and V<sub>2</sub>O<sub>5</sub>, based on the total weight of the glass, and wherein the at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub> is present in an amount sufficient to increase the rate of at least one of crystalline ZrO<sub>2</sub> or crystalline HfO<sub>2</sub> formation from the glass as compared to a comparative glass-ceramic made by heat-treating, in the same manner, the same glass free of Nb<sub>2</sub>O<sub>5</sub> and Ta<sub>2</sub>O<sub>5</sub>.
- The method according to claim 1, wherein the glass comprises ZrO<sub>2</sub>, and
   wherein the at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub> is present in an amount sufficient to increase the rate of crystalline ZrO<sub>2</sub> formation from the glass as compared to the comparative glass-ceramic.
- 3. The method according to claim 2, wherein the at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub>
  20 is present in an amount sufficient to increase the rate of crystalline ZrO<sub>2</sub> formation from the glass by at least a factor of 1.5 as compared to the comparative glass-ceramic.
  - 4. The method according to claim 2, wherein the at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub> is present in an amount sufficient to increase the rate of crystalline ZrO<sub>2</sub> formation from the glass by at least a factor of 2 as compared to the comparative glass-ceramic.
  - 5. The method according to claim 2, wherein the at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub> is present in an amount sufficient to increase the rate of crystalline ZrO<sub>2</sub> formation from the glass by at least a factor of 3 as compared to the comparative glass-ceramic.

- 6. The method according to claim 2, wherein the glass comprises at least 50 percent by weight Al<sub>2</sub>O<sub>3</sub>, based on the total weight of the glass.
- 7. The method according to claim 2, wherein the glass comprises at least 15 percent by weight ZrO<sub>2</sub>, based on the total weight of the glass.
  - 8. The method according to claim 2, wherein the glass comprises at least 20 percent by weight ZrO<sub>2</sub>, based on the total weight of the glass.
- 9. The method according to claim 2, wherein the glass comprises at least 5 percent by weight of at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub>, based on the total weight of the glass.

- 10. The method according to claim 9, wherein the REO is at least one of  $Gd_2O_3$ ,  $La_2O_3$ , or  $Nd_2O_3$ .
- 11. The method according to claim 1, wherein the glass comprises at least 50 percent by weight Al<sub>2</sub>O<sub>3</sub>, at least 30 percent by weight REO, and at least 10 percent by weight ZrO<sub>2</sub>.
- 20 12. The method according to claim 1, wherein the REO is at least one of  $Gd_2O_3$ ,  $La_2O_3$ , or  $Nd_2O_3$ .
  - 13. The method according to claim 1, wherein the glass comprises at least 15 percent by weight ZrO<sub>2</sub>, based on the total weight of the glass.
  - 14. The method according to claim 1, wherein the glass-ceramic has an average hardness of at least 15 GPa.
- 15. The method according to claim 1, further crushing the glass-ceramic to provide abrasive particles.

- 16. The method according to claim 15, further comprises grading the abrasive particles to provide a plurality of particles having a specified nominal grade.
- 17. The method according to claim 15 further comprises incorporating theabrasive particles into an abrasive article.
  - 18. The method according to claim 17, wherein the abrasive article is a bonded abrasive article, a non-woven abrasive article, or a coated abrasive article.
- 10 19. The method according to claim 1, wherein the glass-ceramic has an average hardness of at least 16 GPa.
  - 20. The method according to claim 1, wherein the glass-ceramic has an average hardness of at least 17 GPa.
  - 21. The method according to claim 1, wherein the glass-ceramic has an average hardness of at least 18 GPa.
- 22. The method according to claim 1, wherein the glass-ceramic has an average hardness of at least 19 GPa.

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23. A method for making a glass-ceramic, the method comprising heat-treating ceramic comprising glass to convert at least a portion of the glass to crystalline ceramic and provide glass-ceramic, the glass comprising at least 35 percent by weight Al<sub>2</sub>O<sub>3</sub>, based on the total weight of the glass, REO, at least one of ZrO<sub>2</sub> or HfO<sub>2</sub>, and at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub>, wherein the glass contains not more than 10 percent by weight collectively As<sub>2</sub>O<sub>3</sub>, B<sub>2</sub>O<sub>3</sub>, GeO<sub>2</sub>, P<sub>2</sub>O<sub>5</sub>, SiO<sub>2</sub>, TeO<sub>2</sub>, and V<sub>2</sub>O<sub>5</sub>, based on the total weight of the glass, and wherein the at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub> is present in an amount sufficient to increase the rate of at least one of crystalline ZrO<sub>2</sub> or crystalline HfO<sub>2</sub> formation from the glass as compared to a comparative glass-ceramic made by heat-treating, in the same manner, the same glass free of Nb<sub>2</sub>O<sub>5</sub> and Ta<sub>2</sub>O<sub>5</sub>.

24. The method according to claim 23, wherein the glass comprises  $ZrO_2$ , and wherein the at least one of  $Nb_2O_5$  or  $Ta_2O_5$  is present in an amount sufficient to increase the rate of crystalline  $ZrO_2$  formation from the glass as compared to the comparative glass-ceramic.

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25. The method according to claim 24, wherein the at least one of  $Nb_2O_5$  or  $Ta_2O_5$  is present in an amount sufficient to increase the rate of crystalline  $ZrO_2$  formation from the glass by at least a factor of 2 as compared to the comparative glass-ceramic.

26. The method according to claim 24, wherein the REO is at least one of  $Gd_2O_3$ ,  $La_2O_3$ , or  $Nd_2O_3$ .

- 27. The method according to claim 24, further comprising crushing the glass-15 ceramic to provide abrasive particles.
  - 28. The method according to claim 27, further comprises grading the abrasive particles to provide a plurality of particles having a specified nominal grade.
- 20 29. A method for making an abrasive article, wherein the method according to claim 27 further comprises incorporating the abrasive particles into an abrasive article.
  - 30. A method for making abrasive particles, the method comprising heat-treating glass particles to convert at least a portion of the glass to crystalline ceramic and provide glass-ceramic and the abrasive particles, the glass comprising at least 35 percent by weight Al<sub>2</sub>O<sub>3</sub>, based on the total weight of the glass, REO, at least one of ZrO<sub>2</sub> or HfO<sub>2</sub>, and at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub>, wherein the glass contains not more than 10 percent by weight collectively As<sub>2</sub>O<sub>3</sub>, B<sub>2</sub>O<sub>3</sub>, GeO<sub>2</sub>, P<sub>2</sub>O<sub>5</sub>, SiO<sub>2</sub>, TeO<sub>2</sub>, and V<sub>2</sub>O<sub>5</sub>, based on the total weight of the glass, and wherein the at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub> is present in an amount sufficient to increase the rate of at least one of crystalline ZrO<sub>2</sub> or crystalline HfO<sub>2</sub> formation from the

glass as compared to a comparative glass-ceramic made by heat-treating, in the same manner, the same glass free of  $Nb_2O_5$  and  $Ta_2O_5$ .

31. The method according to claim 30, wherein the glass comprises ZrO<sub>2</sub>, and wherein the at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub> is present in an amount sufficient to increase the rate of crystalline ZrO<sub>2</sub> formation from the glass as compared to the comparative glass-ceramic.

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- 32. The method according to claim 31, wherein the at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub>
  10 is present in an amount sufficient to increase the rate of crystalline ZrO<sub>2</sub> formation from the glass by at least a factor of 1.5 as compared to the comparative glass-ceramic.
  - 33. The method according to claim 31, wherein the at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub> is present in an amount sufficient to increase the rate of crystalline ZrO<sub>2</sub> formation from the glass by at least a factor of 2 as compared to the comparative glass-ceramic.
  - 34. The method according to claim 31, wherein the at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub> is present in an amount sufficient to increase the rate of crystalline ZrO<sub>2</sub> formation from the glass by at least a factor of 3 as compared to the comparative glass-ceramic.
  - 35. The method according to claim 31, wherein the glass comprises at least 50 percent by weight Al<sub>2</sub>O<sub>3</sub>, based on the total weight of the glass.
- 36. The method according to claim 31, wherein the glass comprises at least 15 percent by weight ZrO<sub>2</sub>, based on the total weight of the glass.
  - 37. The method according to claim 31, wherein the glass comprises at least 20 percent by weight ZrO<sub>2</sub>, based on the total weight of the glass.
- 38. The method according to claim 31, wherein the glass comprises at least 5 percent by weight of at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub>, based on the total weight of the glass.

- 39. The method according to claim 38, wherein the REO is at least one of  $Gd_2O_3$ ,  $La_2O_3$ , or  $Nd_2O_3$ .
- 5 40. The method according to claim 31, wherein the glass comprises at least 50 percent by weight Al<sub>2</sub>O<sub>3</sub>, at least 30 percent by weight REO, and at least 10 percent by weight ZrO<sub>2</sub>.
- 41. The method according to claim 31, wherein the REO is at least one of  $Gd_2O_3$ , 10  $La_2O_3$ , or  $Nd_2O_3$ .
  - 42. The method according to claim 31, wherein the glass comprises at least 15 percent by weight ZrO<sub>2</sub>, based on the total weight of the glass.
- 15 43. The method according to claim 31, further comprises grading the abrasive particles to provide a plurality of particles having a specified nominal grade.
  - 44. The method according to claim 31 further comprises incorporating the abrasive particles into an abrasive article.

- 45. The method according to claim 44, wherein the abrasive article is a bonded abrasive article, a non-woven abrasive article, or a coated abrasive article.
- 46. The method according to claim 31, wherein the glass-ceramic has an average hardness of at least 16 GPa.
  - 47. The method according to claim 31, wherein the glass-ceramic has an average hardness of at least 17 GPa.
- The method according to claim 31, wherein the glass-ceramic has an average hardness of at least 18 GPa.

- 49. The method according to claim 31, wherein the glass-ceramic has an average hardness of at least 19 GPa.
- 50. A method for making abrasive particles, the method comprising heat-treating particles comprising glass to convert at least a portion of the glass to crystalline ceramic and provide glass-ceramic and the abrasive particles, the glass comprising at least 35 percent by weight Al<sub>2</sub>O<sub>3</sub>, based on the total weight of the glass, REO, at least one of ZrO<sub>2</sub> or HfO<sub>2</sub>, and at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub>, wherein the glass contains not more than 10 percent by weight collectively As<sub>2</sub>O<sub>3</sub>, B<sub>2</sub>O<sub>3</sub>, GeO<sub>2</sub>, P<sub>2</sub>O<sub>5</sub>, SiO<sub>2</sub>, TeO<sub>2</sub>, and V<sub>2</sub>O<sub>5</sub>, based on the total weight of the glass, and wherein the at least one of Nb<sub>2</sub>O<sub>5</sub> or Ta<sub>2</sub>O<sub>5</sub> is present in an amount sufficient to increase the rate of at least one of crystalline ZrO<sub>2</sub> or crystalline HfO<sub>2</sub> formation from the glass as compared to a comparative glass-ceramic made by heat-treating, in the same manner, the same glass free of Nb<sub>2</sub>O<sub>5</sub> and Ta<sub>2</sub>O<sub>5</sub>.

51. The method according to claim 50, wherein the glass comprises  $ZrO_2$ , and wherein the at least one of  $Nb_2O_5$  or  $Ta_2O_5$  is present in an amount sufficient to increase the rate of crystalline  $ZrO_2$  formation from the glass as compared to the comparative glass-ceramic.

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- 52. The method according to claim 51, wherein the at least one of  $Nb_2O_5$  or  $Ta_2O_5$  is present in an amount sufficient to increase the rate of crystalline  $ZrO_2$  formation from the glass by at least a factor of 2 as compared to the comparative glass-ceramic.
- 25 53. The method according to claim 51, wherein the REO is at least one of  $Gd_2O_3$ ,  $La_2O_3$ , or  $Nd_2O_3$ .
  - 54. The method according to claim 51, further comprises grading the abrasive particles to provide a plurality of particles having a specified nominal grade.

55. A method for making an abrasive article, wherein the method according to claim 51 further comprises incorporating the ceramic abrasive particles into an abrasive article.